

59. $D < 0$

$\Rightarrow px^2 + qx + r$ is always positive or always negative

But Given $f(2) > 0$

$\Rightarrow f(0)$ and $f(1)$ are also > 0

$\Rightarrow r > 0$ & $p + q + r > 0$

60.
$$I_n = \int_{-\pi}^0 \frac{\sin(nx)}{(1+\pi^x)\sin(x)} dx + \int_0^{\pi} \frac{\sin(nx)}{(1+\pi^x)\sin(x)} dx$$

$$= \int_{\pi}^0 \frac{\sin(nx)}{(1+\pi^{-x})\sin(-x)} d(-x) + \int_0^{\pi} \frac{\sin(nx)}{(1+\pi^x)\sin(x)} dx$$

$$= \int_0^{\pi} \frac{\sin(nx)}{\sin x} \left\{ \frac{1}{1+\pi^x} + \frac{1}{1+\pi^x} \right\} dx$$

$$I_n = \int_0^{\pi} \frac{\sin(nx)}{\sin(x)} dx$$

$$I_{n+2} - I_n = 0$$

$$\Rightarrow I_{n+2} = I_n$$

$$I_5 = I_3 = I_1 \text{ etc}$$

$$I_4 = I_2 = I_0 \text{ etc}$$

$$\sum_{m=1}^{10} I_{2m+1} = I_3 + I_5 + \dots + I_{21}$$

$$I_1 + I_1 \dots 10 \text{ times}$$

$$10I_1 = 10\pi$$

$$\sum_{m=1}^{10} I_{2m} = I_0 + I_0 + \dots 10 \text{ times}$$

$$= 10I_0 = 0$$
